Lecture 1, Jan 9, 2024

Types of Learning

- Supervised learning: given a training inputs and training targets, we want to learn a relationship for prediction purposes

 - Input data is specified as pairs: $\left\{ \left(\boldsymbol{x}^{(i)}, \boldsymbol{y}^{(i)} \right) \right\}_{i=1}^{N}$ e.g. regression, classification, time series forecasting, even learning governing equations
 - Main goal is to make predictions
- Unsupervised learning: given training data without labels (targets), we want to learn meaningful patterns in the data
 - e.g. clustering, probability density estimation, dimensionality reduction, generative AI models
- Semi-supervised learning: targets are only known for a small subset of the training inputs
- Reinforcement learning: an agent continuously interacting with the environment learning to maximize a reward function
 - This is an approach for sequential decision making

Parameter Estimation

- Frequentist approach: estimate the model parameters by minimizing a loss function, resulting in a single point in parameter space \boldsymbol{w}
 - e.g. regression using least squares
- Bayesian approach: estimate the posterior distribution of the parameters using Bayes' theorem
 - This allows us to also estimate the uncertainty in the model
 - Frequentist estimation is more efficient, but carries no information about the uncertainty