

# Lecture 11, Feb 3, 2023

## Effect of Electric Field on Materials

- If an external electric field is applied to a material, then “excess” or “mobile” charges will be pushed along by the field
- Based on the amount of mobile charges, most materials fall into 3 categories: conductors, semiconductors, and dielectrics (insulators)
  - In a conductor the band gap is very small so very little energy is needed to promote an electron to the conduction band
  - In a dielectric the band gap is quite large, so a lot of energy is needed for conduction
- The movement of charges creates a current  $I$ ; we can define a *current density*  $J$  so that  $I = \iint_S \vec{J} \cdot d\vec{S}$ 
  - $\vec{J}$  has units of A/m<sup>2</sup>

### Equation

The relationship between current density and an electric field causing the current is

$$\vec{J} = \sigma \vec{E}$$

where  $\sigma$  is the conductivity of the material

- This is known as Ohm’s law in microscopic (point) form
- Conductivity characterizes how easily a current flows within that material
  - Later we see  $\sigma = \frac{N_e e^2 \tau}{m_e}$  where  $N_e$  is the electron density and  $\tau$  is the mean free time
  - In general  $\sigma$  goes down as temperature goes up as  $\tau$  decreases when the atoms become more energetic
- Resistivity is the inverse of conductivity,  $\rho = \frac{1}{\sigma}$  with units of  $\Omega$  m
- Properties of perfect conductors and dielectrics:
  - In a perfect conductor,  $\sigma \rightarrow \infty$ , so no applied field is needed for current to flow, and *there is always zero electric field*
  - In a perfect insulator,  $\sigma \rightarrow 0$ , so there is never any current; the electric field can be anything but the material will not respond
- A perfect conductor will have the same potential everywhere on its surface, so all perfect conducting surfaces are equipotential; therefore the electric field is always perpendicular to them