

## Lecture 9, Nov 15, 2023

### Taxation

- Companies are taxed based on taxable income, which revenues minus expenses
  - We will use a flat tax rate
- Revenues can include any income made by the company:
  - Sales revenues
  - Interest revenues
  - Capital gains (selling an asset above its book value)
    - \* In accounting, the true price of an asset is its book value, so the difference is counted as taxable income
- Expenses and deductions reduce the amount of taxable income:
  - Cost of goods sold
  - SG&A
  - Interest expenses
  - Depreciation expenses
  - Capital losses (selling an asset below its book value)
- Not all expenses are counted towards taxes, e.g. dividends, asset purchases and some others are not counted
  - Asset purchases are not counted because they still have value after you purchase them, so that money is not considered “consumed”
    - \* Therefore taxes don’t affect first costs
  - However after purchase, depreciation and capital gains/losses do affect taxes
  - In general if something does not show up on the income statement (i.e. only balance sheet), it does not affect taxes
- Rate of returns are discounted by the tax rate for cash flows after tax, because we expect less profit
  - MARR and IRR after tax is the pre-tax rate multiplied by 1 minus the tax rate (as an approximation)
    - \* This gives the WACC
  - Note that equity rates (i.e. numbers from CAPM) are after-tax; so we don’t need to adjust these
  - $R_{WACC} = \frac{E}{E+D}R_E + \frac{D}{E+D}R_D(1-t)$ 
    - \* Only the debt rate is discounted by tax

### Capital Cost Allowance (CCA)

- Depreciation is not a real cash flow, but claiming depreciation saves on taxes
  - A company will want to depreciate as much as possible, as fast as possible due to time value of money
  - Government regulations exist to make sure companies can’t arbitrarily depreciate
  - Note that on the actual balance sheet, a company might want to depreciate more slowly because this makes their income look better, but for tax purposes they must use CCA; this results in a discrepancy on the balance sheet
- CCA is the Canadian system for calculating depreciation and taxes
  - The capital cost allowance (CCA) is the amount of depreciation
  - The undepreciated capital cost (UCC) is the book value
  - The proceeds from disposition is the salvage value from selling the asset
- Assets are pooled into classes specified by the policy
  - All assets are pooled into classes, and the total value of all assets in each class is depreciated together at some specified rate
    - \* Assets are not depreciated individually
  - The depreciation method is similar to declining balance, but new assets purchased this year are only depreciated at half the rate
    - \*  $CCA = CCA \text{ rate times } (\text{new assets this year} / 2 + \text{UCC from last year})$

- \* This is known as the half-year rule
  - UCC this year is UCC from last year, plus new assets this year, minus CCA
- The amount of tax savings each year is the CCA from that year times the tax rate; this is recorded as a positive cash flow
- When selling the asset, the book value can be different from the salvage value
  - *Open book*: other items exit in the same CCA pool
    - \* Selling the asset does not close out the pool
    - \* Simply reduce the UCC of the pool by the salvage value
  - *Closed book*: no other items in the same pool; there are 3 cases:
    - \* *Terminal loss*: salvage value less than book value
      - Claim the loss, book value minus salvage value, which decreases taxable income
    - \* *Recapture*: salvage value greater than book value, but less than original price
      - Report the recapture, salvage value minus book value, which increases taxable income
    - \* *Capital gains*: salvage value greater than the original price
      - Report the recapture, original price minus book value, which increases taxable income
- Example: purchasing \$5000 worth of desks (class 8, CCA rate of 20%); what are the CCA and UCC for the first 4 years, assuming there is nothing in the same pool?
  - First year: \$5000 in purchases, no UCC from last year, CCA is 20% of \$5000 divided by 2 = \$500, so we're left with \$4500
  - Second year: \$0 in purchases, \$4500 from last year, CCA is 20% of \$4500 = \$900, so we're left with 3600
  - This gives us \$2304 at the end of the 4th year
  - In year 5, we sell the desks for \$1500; what is the gain/loss as a result of selling the desks, assuming open book?
    - \* CCA in year 5 is \$460
    - \* UCC after year 5 is \$2304, minus the CCA and minus the \$1500 sell value
    - \* Since this is open book, we have no direct gains or losses, so no direct tax implications
  - What if there are no other assets in class 8?
    - \* Since the UCC must go to 0, the book value for the desks would be \$2304 minus UCC, or \$1844
    - \* We sold it for a loss, so we can claim a loss of \$344, which is a tax saving
  - What if we sold it for \$2500?
    - \* This is greater than book value, so we have a recapture of \$2500 - \$1844 = \$656
    - \* This makes the taxes go up

## Calculating Present Worth

- Using the explicit method:
  - Use the WACC (after-tax discounted MARR)
  - Revenues are discounted by the tax rate
  - No changes to first costs
  - Take into account depreciation tax savings every year by calculating CCA every year
  - Account for terminal losses or gains by comparing the final UCC to the salvage value, in a closed-book scenario
- The *tax benefit factor*  $\tau$  is defined as the ratio of the present worth of tax savings to the first cost of equipment
  - Assets have inherent value but also value associated with tax benefits
  - $\tau$  is how much every dollar spent will save in taxes
    - \* Note that this assumes we will keep the asset around forever, so we get the tax savings for the rest of time
  - This depends on the depreciation method, tax rate, WACC, etc
  - For regular declining balance,  $\tau_{db} = \frac{td}{i+d}$  where  $i$  is the after-tax WACC,  $d$  is the depreciation rate and  $t$  is the tax rate
    - \* This applies to asset disposition

- For declining balance with half-year rule,  $\tau_{1/2} = \frac{td}{i+d} \left( \frac{1 + \frac{i}{2}}{1+i} \right)$ 
  - \* This applies to asset purchases
- Using tax benefit factors, the *effective first cost* is reduced because of tax savings
  - $PW(FC) = -FC + FC\tau_{1/2} = -FC(1 - \tau_{1/2})$
  - The term  $(1 - \tau_{1/2})$  is known as the *capital tax factor* (CTF)
- The *effective salvage value* of selling an asset is reduced because of losing tax savings
  - Since the CTF assumes we keep the tax forever, when we actually sell the asset we need to correct for the tax savings that we lose
  - $PW(S) = (S - R\tau_{ab})(P/F, i, N)$
  - $S$  is the salvage value,  $R$  is the reduction in the pool due to selling the asset
  - The term  $(1 - \tau_{ab})$  is known as the *capital salvage factor* (CSF)
- Using tax benefit factors we can calculate present worth as:
  - Use the effective first cost
  - Discount revenues by the tax rate
  - Use the effective salvage value, which depends on whether we have an open or closed book scenario
    - \* For open-book,  $R = S$ , so  $PW(S) = S(1 - \tau_{ab})(P/F, i, N)$
    - \* For closed-book,  $R = UCC$ , and we also need to account for possible terminal loss/gain