## Lecture 17, Feb 18, 2022

## Superposition Principle

- Linear circuit: A circuit that consists of independent sources, linear dependent sources, and linear elements
  - Examples of linear elements include resistors, capacitors and inductors
- Superposition principle: The response of a linear circuit to multiple independent sources is equal to the algebraic sum of the responses caused by each independent source acting alone
- This allows us to look at only one independent source at a time to simplify the problem
- Example circuit: Find the voltage  $v_x$ :

$$6V \stackrel{+}{\xrightarrow{-}} v_x \stackrel{+}{\underset{-}{\overset{-}}} 4\Omega \quad \textcircled{3A}$$

- Phase 1: Deactivate the voltage source

\* To deactivate a voltage source, we short it out so the voltage is zero:

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\* Now the resistors are in parallel; use current division:  $i_{x_1} = 3\frac{8}{4+8} = 2A$ , so  $v_{x_1} = 4i_{x_1} = 8V$ 

- Phase 2: Deactivate the current source
  - \* To deactivate a current source, we open the circuit so the current is zero:



\* Now the resistors are in series; use voltage division:  $v_{x_2} = 6\frac{4}{4+8} = 2V$ - The voltage across  $v_x$  with the two sources combined is  $v_x = v_{x_1} + v_{x_2} = 10V$