Lecture 9, Sep 27, 2022

Additional Verilog Statements

- always block
 - Statements in an always block execute sequentially
 - In an always block, we don't use assign
 - = (as opposed to assign) is a blocking assignment; must be used inside always blocks and enforces sequential execution order
- Conditionals such as if/else/else if must exist in an always block
 - if without else generates a latch

endmodule

- case statements
 - Can be used to do pattern matching
 - Instead of deriving a logic expression, we can let Verilog do it for us
 - Also needs to be inside an <code>always</code> block
 - default catches unspecified cases; without this the compiler will generate latches (more on this later)

Karnaugh Maps (K-Maps)

- A method of optimizing logic expressions
- The point of logic simplification is to reduce the cost (area) of a circuit; for our purposes, our metric for cost is the number of gates and inputs
 - $-\cos t = \# \text{ of gates} + \# \text{ of inputs}$
- Optimization using boolean algebra is awkward and error prone
 - When optimizing using boolean algebra, we need to combine terms, but seeing that those combinations are possible is challenging
- Karnaugh Maps are a type of truth table in which minterms that cam be combined are adjacent
- Example: 2-variable K-Map

x_1	0	1
0	m_0	m_2
1	m_1	m_3

- Looking at the first column, $f = m_0 + m_1 = \bar{x}_1 \bar{x}_2 + \bar{x}_1 x_2 = \bar{x}_1$ - The second row: $f_2 = m_1 + m_2 = \bar{x}_1 x_2 + x_1 x_2 = x_2$ - Example: $f(x_1, x_2) = \sum m(0, 1, 3)$

$$-f = \bar{x}_1 \bar{x}_2 + \bar{x}_1 x_2 + x_1 \bar{x}_2$$

* As it is the circuit has a cost of 17 (3 AND, 1 3-input OR, 2 NOT + 2 inputs per AND, 3 inputs per OR, 1 input per NOT)

– K-Map:

x_1	0	1
0	1	0
1	1	1

- This lets us simplify our circuit to $f = \bar{x}_1 + x_2$ which only has a cost of 5
- To simplify using a K-Map, we group adjacent minterms in the map
 - The second row shows that regardless of x_1 , as long as x_2 is 1, the expression is 1, so that row simplifies to x_2
 - The first column shows that regardless of x_2 , as long as x_1 is 0, the expression is 1, so the row simplifies to \bar{x}_1
- We can only group terms in group sizes of powers of 2 (for a 2×2 K-Map, we can group 2 terms or 4 terms)