

Formula	Description	Formula	Description
<b>Suspension Bridges</b>		<b>Trusses</b>	
$T_y = \frac{wL}{2}, T_x = \frac{wL^2}{8h}$	Main cable tension in suspension bridge	$P_e = \frac{\pi^2 EI}{L^2}$	Euler buckling load
<b>Basic Material Properties</b>		$r = \sqrt{\frac{I}{A}}$	Definition: Radius of gyration
$\sigma = \frac{P}{A}$	Definition: Stress	$\frac{L}{r}$	Definition: Slenderness ratio
$\varepsilon = \frac{\Delta l}{l_0}$	Definition: Strain	$F^* \Delta = \sum_{i=1}^n P_i^* \Delta l_i$	Virtual work; $F^*$ is the <b>virtual</b> force applied, $\Delta$ is the <b>real</b> displacement in the same direction, $P_i^*$ are the loads caused by the <b>virtual</b> force, $\Delta l_i$ are the <b>real</b> changes in length.
$E = \frac{\sigma}{\varepsilon}, \sigma = E\varepsilon$	Definition: Young's Modulus	<b>Factors of Safety</b>	
$\mu = \nu = -\frac{\varepsilon_y}{\varepsilon_x}$	Definition: Poisson's Ratio	$\text{FoS} = \frac{\text{Capacity}}{\text{Demand}}$	Definition: Factor of Safety
$k = \frac{AE}{L_0}$	Spring constant from Young's modulus	$A \geq \text{FoS}_y \frac{P}{\sigma_y}$	Cross-sectional area requirement against yield; $\text{FoS}_y$ typically 2.0
$\varepsilon_{th} = \alpha \Delta T$	Strain from thermal expansion	$I \geq \text{FoS}_b \frac{PL^2}{\pi^2 E}$	Second moment of area requirement against buckling; $\text{FoS}_b$ typically 3.0
<b>Energy</b>		$r \geq \frac{L}{200}$	Radius of gyration requirement to prevent slender members
$W = \int F d\Delta l$	Definition: Strain energy	<b>Bending of Beams</b>	
$U = \int \sigma d\varepsilon, W = U \cdot V_0$	Definition: Strain energy density	$\phi = \frac{d\theta}{dx} = \frac{d^2 y}{dx^2}$	Definition: Curvature (small angles)
$W = \frac{1}{2} \sigma \varepsilon V_0$	Strain energy when material is linear elastic	$M = EI \cdot \phi, \phi = \frac{M}{EI}$	Bending moment and flexural stiffness $EI$
<b>Second Moment of Area and Centroid</b>		$\sigma = \frac{My}{I}$	Navier's Equation (flexural stresses); $y$ is distance from centroidal axis
$I = \int_A y^2 dA$	Definition: Second moment of area	$\Delta V_{AB} = \int_A^B w(x) dx$	Relationship between shear force and vertical loads
$I_m = \int_A y^2 dm = \rho I$	Definition: Moment of inertia	$\Delta M_{AB} = \int_A^B V(x) dx$	Relationship between bending moment and shear force
$I = \frac{bh^3}{12}$	$I$ for rectangular cross section	$\Delta \theta_{AB} = \int_A^B \phi(x) dx$	Moment Area Theorem 1
$I = \frac{\pi d^4}{64}$	$I$ for circular cross section ( $d$ is diameter, horizontal axis)	$\delta_{BA} = \bar{x}_{BA} \int_A^B \phi(x) dx$	Moment Area Theorem 2; $\delta_{BA}$ is the tangential deviation at point $B$ from a tangent at $A$ , $\bar{x}_{BA}$ is the horizontal distance of point $B$ from the centroid of the area under $\phi(x)$ from $A$ to $B$
$I = \sum_{i=1}^n (I_{0,i} + A_i d_i^2)$	Parallel axis theorem; $I_0$ is $I$ about the local centroid, $A$ is the area, and $d_i$ is the distance between the local and global centroids	<b>Shear Stresses</b>	
$\bar{y} = \frac{1}{A} \sum_{i=1}^n y_i A_i$	Centroidal axis location	$\tau = \frac{V}{A}$	Definition: Shear stress
<b>Oscillations and Dynamic Effects</b>		$\tau = \frac{VQ}{Ib}$	Jourawski's Equation; $b$ is the width of the cross section at the depth of interest, $Q$ is a first moment of area about the centroid
$\omega_n = \sqrt{\frac{k}{m}}$	Natural angular frequency		
$f_n = \frac{15.76}{\sqrt{\Delta_0}}$	Natural frequency, point load		
$f_n = \frac{17.76}{\sqrt{\Delta_0}}$	Natural frequency, distributed load		
$\frac{1}{\sqrt{(1-\alpha^2)^2 + (2\beta\alpha)^2}}$	Dynamic amplification factor; $\alpha = \frac{f}{f_n}$ ; $\beta$ is the damping ratio		
$w_{eq} = w_{sta} + \text{DAF} \cdot w_0$	Equivalent dynamic load		

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<b>Shear Stresses (Contd.)</b>		<b>Stone and Concrete (Contd.)<sup>1</sup></b>	
$Q = \int_{y_{bot}}^{y_0} y dA$ $= \int_{y_0}^{y_{top}} y dA$	First moment of area in Jourawski's Equation; $y_0$ is the depth of interest	$k = \sqrt{(n\rho)^2 + 2n\rho} - n\rho$	Neutral axis location of cracked reinforced concrete; $kd$ is the distance from the compression side of the member to the neutral axis
$Q = \sum_{i=1}^n A_i d_i$	Calculating $Q$ by breaking it up into smaller areas	$j = 1 - \frac{1}{3}k$	Flexural lever arm; $jd$ is the distance between the compressive and tensile forces
<b>Local Buckling</b>		$f_s = \frac{M}{A_s j d}$	Tensile stress in the steel rebar under bending
$\sigma = \frac{\pi^2 E}{12} \left( \frac{t}{L} \right)^2$	Euler buckling of a plate with thickness $t$ length $L$ and Young's modulus $E$ , with both sides unrestrained	$f_c = \frac{k}{1-k} \frac{M}{n A_s j d}$	Compressive stress in the concrete under bending; $n$ is the modular ratio
$\sigma = \frac{k \pi^2 E}{12(1-\mu^2)} \left( \frac{t}{b} \right)^2$	General local buckling equation for a plate with thickness $t$ , width $b$ ( $b > t$ ), and Poisson's ratio $\mu$ ; $k$ depends on boundary conditions	$v = \frac{V}{b_w j d}$	Maximum shear stress in cracked concrete; $V$ is the shear force, $b_w$ is the effective web width (may consider adjacent webs)
$k = 4$	When both edges of the plate are restrained from buckling out of plane (middle flange)	$v_{max} = 0.25 f'_c$ $V_{max} = 0.25 f'_c b_w j d$	Shear stress/force that causes failure by diagonal crushing of the concrete
$k = 0.425$	When only one edge of the plate is restrained from buckling out of plane (side flange)	$v_c = \frac{230 \sqrt{f'_c}}{1000 + 0.9d}$ $V_c = \frac{230 \sqrt{f'_c}}{1000 + 0.9d} b_w j d$	Shear strength of concrete without shear reinforcement (aggregate interlock only)
$k = 6$	When stress is linear from 0 to $\sigma_{crit}$ and both sides of the plate are restrained (webs)	$v_s = \frac{A_v f_y}{b_w s} \cot 35^\circ$ $V_s = \frac{A_v f_y j d}{s} \cot 35^\circ$	Shear strength of shear reinforcement; $A_v$ is the total area of shear reinforcement, $s$ is the spacing between shear reinforcement bars, $f_y$ is the yield strength of the steel
$\tau = \frac{5\pi^2 E}{12(1-\mu^2)} \cdot \left( \left( \frac{t}{h} \right)^2 + \left( \frac{t}{a} \right)^2 \right)$	Shear buckling stress; $h$ is the height of the plate, $a$ is the horizontal distance between stiffeners (diaphragms)	<b>Stone and Concrete<sup>1</sup></b>	
$M = Pe$ $\sigma = \frac{P}{A} + \frac{My}{I}$	Combined axial and bending stress from load $P$ misaligned from the centroidal axis by distance $e$	$\frac{A_v f_y}{b_w s} \geq 0.06 \sqrt{f'_c}$	Threshold for shear reinforcement, above which the equations below should be used for $v_c$ and $V_c$ instead
$f'_t = 0.33 \sqrt{f'_c}$	Tensile strength of concrete from compressive strength	$v_c = 0.18 \sqrt{f'_c}$ $V_c = 0.18 \sqrt{f'_c} b_w j d$	Shear strength of concrete if there is enough shear reinforcement to satisfy the equation above
$E_c = 4730 \sqrt{f'_c}$	Young's modulus of concrete from compressive strength	$V_r = 0.5 V_c + 0.6 V_s$ $\leq 0.5 V_{max}$	Overall shear strength including factors of safety (concrete terms are multiplied by 0.5, steel terms 0.6); $V_{max}$ is the shear force causing concrete crushing
$n = \frac{E_s}{E_c}$	Definition: Modular ratio; $E_s$ is the Young's modulus of steel, $E_c$ is the Young's modulus of concrete		
$\rho = \frac{A_s}{bd}$	Definition: Longitudinal reinforcement density; $A_s$ is the total area of reinforcing steel, $b$ is the width of the compression side of the member, $d$ is the effective depth of the rebar		

<sup>1</sup>For all equations involving  $\sqrt{f'_c}$ , standard units of MPa, mm and N **must** be used.